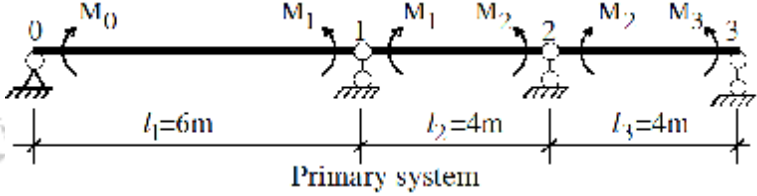
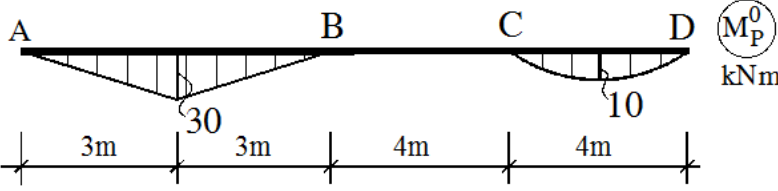
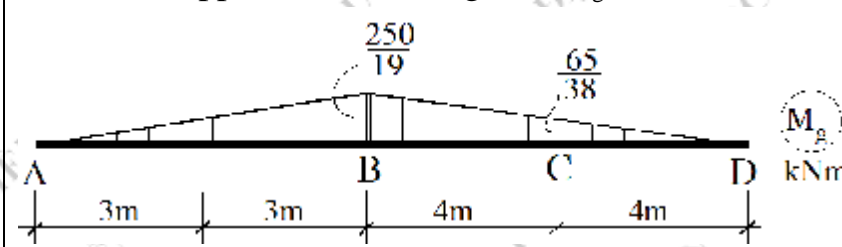
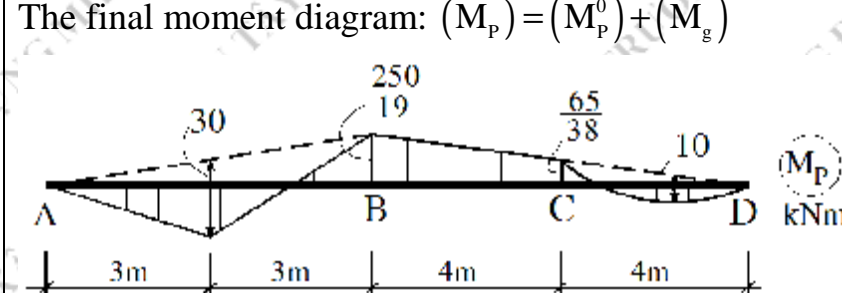
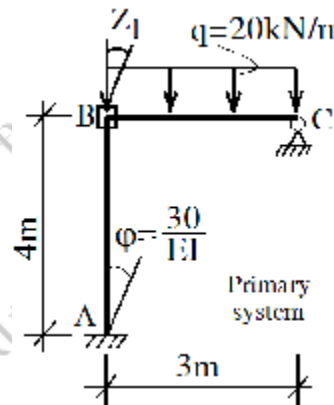


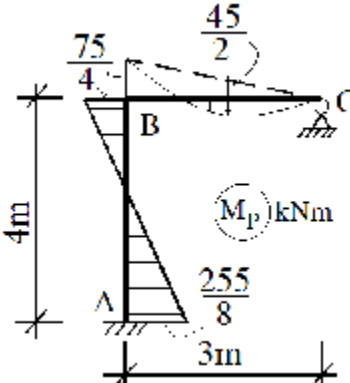
ĐÁP ÁN ĐỀ THI CHÍNH THỨC

Solution:

Problem 1	Part	Content	Marks
		Determine degree of static indeterminacy: $n = C - 3 = 5 - 3 = 2$	0,25
		Draw the simple beam free-body diagram for each span of the beam, label the spans, label the supports, and primary system 	0,5
		Draw the bending moment diagram for each span of the simple beam, M_p^0 	0,5
		Use the three-moment equation for the support 1 $l_1 M_0 + 2(l_1 + l_2) M_1 + l_2 M_2 = -6 \left(\frac{w_1 a_1}{l_1} + \frac{w_2 b_2}{l_2} \right)$	0,5
		Use the three-moment equation for the support 2 $l_2 M_1 + 2(l_2 + l_3) M_2 + l_3 M_3 = -6 \left(\frac{w_2 a_2}{l_2} + \frac{w_3 b_3}{l_3} \right)$	0,5
		With: $M_0 = M_3 = 0$ $w_1 a_1 = \frac{1}{2} \times 30 \times 6 \times 3 = 270 \text{ (kNm}^3\text{)}$	0,25
		$w_2 b_2 = w_2 a_2 = 0$	0,25
		$w_3 b_3 = \frac{2}{3} \times 10 \times 4 \times 2 = \frac{160}{3} \text{ (kNm}^3\text{)}$	0,25
		Solve the system of equations	0,25

		$\begin{cases} 20M_1 + 4M_2 = -270 \\ 4M_1 + 16M_2 = -80 \end{cases}$ $\Rightarrow \begin{cases} M_1 = -\frac{250}{19} \text{ (kNm)} \\ M_2 = -\frac{65}{38} \text{ (kNm)} \end{cases}$	
		<p>Draw the support moment diagram, M_g</p> 	0,25
		<p>The final moment diagram: $(M_p) = (M_p^0) + (M_g)$</p> 	0,5
Marks obtained for problem 1			4 points
Problem 2	Part	Content	Marks
		<p>Determine the degree of kinematical indeterminacy:</p> $n = n_1 + n_2 = 1 + 0 = 1$	0,5
		<p>Let us choose the primary system:</p> 	0,5
		<p>The canonical equation of the displacement method is:</p> $r_{11}Z_1 + R_{1p} + R_{1j} = 0$	0,5
		<p>Construct the bending moment diagrams: $\overline{M}_1, M_p^0, M_j^0$</p>	0,5

			0,5
			0,5
		<p>Calculate the main and secondary unit reactions:</p> <p>+ r_{11}:</p> <p>$\Rightarrow r_{11} = 2EI$</p>	0,5
		<p>+ R_{1P}:</p> <p>$\Rightarrow R_{1P} = -\frac{45}{2} (kNm)$</p>	0,5
		<p>+ $R_{1\phi}$:</p> <p>$\Rightarrow R_{1j} = 15 (kNm)$</p>	0,5

		<p>Solve the equation:</p> $2EI Z_1 = \frac{15}{2} \Rightarrow Z_1 = \frac{15}{4EI} \text{ (rad)}$	0,5
		<p>The final bending moment diagram is constructed by a formula:</p> $M_p = \overline{M}_1 Z_1 + M_p^0 + M_j^0$	0,5
			0,5
Marks obtained for problem 2			6 points